

Short communication

# Thermochemistry of potassium strontium tetraborate decahydrate

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## Abstract

The enthalpies of solution of  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}(\text{cr})$  in approximately  $1 \text{ mol dm}^{-3}$  aqueous hydrochloric acid and of  $\text{SrCl}_2 \cdot 6\text{H}_2\text{O}(\text{cr})$  in aqueous solution (hydrochloric acid + boric acid + potassium chloride) were measured by solution calorimetry. From these results and other data, the standard molar enthalpy of formation  $\Delta_f H_m^\circ$  of  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}(\text{cr})$  has been derived to be  $-(10904.47 \pm 6.46) \text{ kJ mol}^{-1}$  at 298.15 K. According to a group contribution method, the standard molar Gibbs free energy  $\Delta_f G_m^\circ$  and the standard molar entropy  $S_m^\circ$  of  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}(\text{cr})$  were also calculated to be  $-9690.78 \text{ kJ mol}^{-1}$  and  $858.31 \text{ J K}^{-1} \text{ mol}^{-1}$  at 298.15 K.

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**Keywords:**  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}$ ; Standard molar enthalpy of formation; Solution calorimetry; Molar enthalpy of solution; Aqueous hydrochloric acid solution

## 1. Introduction

The synthesis, structural, and dehydration studies of borates have attracted a great attention in past few years because of their valuable nonlinear optical (NLO) properties [1]. Until now, eight double tetraborates hydrated, namely  $\text{K}_{1.67}\text{Na}_{0.33}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 3\text{H}_2\text{O}$  [2],  $\text{NaRb}[\text{B}_4\text{O}_5(\text{OH})_4] \cdot 4\text{H}_2\text{O}$  [3],  $\text{K}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [4],  $\text{Rb}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [5],  $\text{Cs}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [6],  $(\text{NH}_4)_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [7],  $\text{Rb}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [8], and  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}$  [7] have been synthesized in this laboratory and their crystal structures established. In previous papers, the thermodynamic properties of three double hydrated borates, namely Ulexite ( $\text{NaCaB}_5\text{O}_6(\text{OH})_6 \cdot 5\text{H}_2\text{O}$ ) [9],  $\text{K}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [10],  $\text{Rb}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [11], and  $\text{Cs}_2\text{Ca}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 8\text{H}_2\text{O}$  [12] have been studied. In this paper, the standard molar enthalpy of formation of  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}$  has been determined by solution calorimetry and other thermochemical parameters have been calculated.

## 2. Experimental

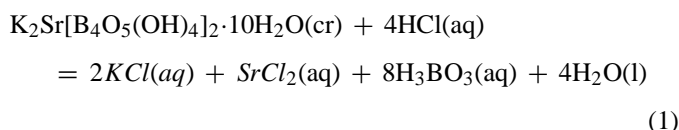
All the reagents used in the synthesis were analytic grade, 12.5 g of a KOH and 25 g  $\text{H}_3\text{BO}_3$  were dissolved in approximately 100 ml  $\text{H}_2\text{O}$  at room temperature, the above solution was mixed with 2.66 g of a  $\text{SrCl}_2 \cdot 6\text{H}_2\text{O}$  dissolved in 10 ml  $\text{H}_2\text{O}$  to form an amorphous precipitate, the mixture was stirred during 20 min and brought to room temperature. The crystal hydrated mixed borate  $\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}$  was obtained in a few days. The compound was characterized by chemical analysis, powder X-ray diffraction, FT-IR spectrum, Raman spectrum and thermal analysis. The powder X-ray diffraction data of the synthesized compound was obtained using Rigaku D/MAX-2400 with  $\text{Cu K}\alpha$  radiation ( $\lambda = 1.5418 \text{ \AA}$ ). FT-IR spectra were recorded in the  $4000\text{--}400 \text{ cm}^{-1}$  region on a Nicolet NEXUS 670 FT-IR spectrometer using KBr pellets; Raman spectra on a Nicolet Omega Dispersive Raman spectrometer. Thermogravimetric analysis (TGA) and DSC were conducted on a NETZSCH-Gerätebau STA 449c, in a flow of  $\text{N}_2$  with a heating rate of  $10 \text{ }^\circ\text{C min}^{-1}$ .

The thermogram indicates a continuous weight loss in the intervals  $50\text{--}500 \text{ }^\circ\text{C}$  with a slope change at  $79.8 \text{ }^\circ\text{C}$ . This loss corresponds to the release of the ten free water molecules and four hydroxyl groups. The observed weight loss (34.71%) is in good agreement with the calculated value (34.60%). The DSC curve shows that there are two exothermic peaks ( $79.8, 857.3 \text{ }^\circ\text{C}$ ) and one endothermic peaks ( $595.4 \text{ }^\circ\text{C}$ ).

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Both chemical analysis and thermal analysis show that double borate hydrated contains 12.91 (cal. 12.93) wt% K<sub>2</sub>O, 14.17 (cal. 14.23) wt% SrO, 38.21 (cal. 38.24) wt% B<sub>2</sub>O<sub>3</sub> and 34.71 (cal. 34.60) wt% H<sub>2</sub>O. The data shows that the compound obtained is pure and has the general formula K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O and is suitable for calorimetric measurements.

To obtain the standard molar enthalpy of formation of hydrated potassium strontium tetraborate, a thermochemical scheme was designed. The enthalpy of solution of K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(s)(cr) in approximately 1 mol dm<sup>-3</sup> aqueous hydrochloric acid solution was determined according to the following equation:



In addition, the H<sub>3</sub>BO<sub>3</sub>(cr) were dissolved in approximately 1 mol dm<sup>-3</sup> aqueous hydrochloric acid, the calculated amount of KCl(cr) was dissolved in aqueous solution (hydrochloric acid + boric acid) which consisted of approximately 1 mol dm<sup>-3</sup> HCl(aq) and the calculated amount of H<sub>3</sub>BO<sub>3</sub>(cr), and then the calculated amount SrCl<sub>2</sub>·6H<sub>2</sub>O(cr) was dissolved in the former mixed solution (hydrochloric acid + boric acid + potassium chloride). Combining with other auxiliary data, the standard molar enthalpies of SrCl<sub>2</sub>·6H<sub>2</sub>O(cr), KCl(cr), H<sub>3</sub>BO<sub>3</sub>(cr) and H<sub>2</sub>O(l), the standard molar enthalpy of K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(cr) could be derived.

The KCl (mass fraction > 0.9999, PR China), H<sub>3</sub>BO<sub>3</sub> (mass fraction > 0.9999, PR China) and SrCl<sub>2</sub>·6H<sub>2</sub>O (mass fraction > 0.9999, PR China) were used without further purification. The HCl standard solution was prepared from azeotropic hydrochloric acid and deionized water, and its concentration was determined by titration with standardized sodium carbonate.

An RD496-III microcalorimeter (built in the Southwest Institute of Electronic Engineering, PR China) was used for calorimetric determinations. The instrument was calibrated by Joule effect, and the accuracy and precision were determined by chemical calibration. The enthalpy of solution of KCl in deionized water was measured at *T* = 298.15 K.

The experimental value (17.24 ± 0.06) kJ mol<sup>-1</sup> agrees with the value (17.241 ± 0.018) kJ mol<sup>-1</sup> reported in the literature [13]. The temperature of the calorimetric experiments was 298.15 ± 0.05 K. A detailed description of procedure is given elsewhere [14]. No solid residues were observed in the solution after the calorimetric experiments.

### 3. Results and discussion

The results are given in Table 1.

According to the group contribution method [19], the Δ<sub>f</sub>H<sub>m</sub><sup>o</sup> and Δ<sub>f</sub>G<sub>m</sub><sup>o</sup> of a hydrated borate should be the sum of contributions of the corresponding cations in an aqueous solution, of the polyborate anions, and of structural water. The Δ<sub>f</sub>H<sub>m</sub><sup>o</sup> and Δ<sub>f</sub>G<sub>m</sub><sup>o</sup> of hydrated mixed borate, K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O could be expressed by Eqs. (2) and (3):

$$\begin{aligned} \Delta_f H_m^o(\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}) \\ = 2\Delta_f H_m^o(\text{K}^+, \text{aq}) + \Delta_f H_m^o(\text{Sr}^{2+}, \text{aq}) \\ + 2\Delta_f H_m^o\{[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}\} + 10\Delta_f H_m^o(\text{H}_2\text{O}, \text{l}) \end{aligned} \quad (2)$$

$$\begin{aligned} \Delta_f G_m^o(\text{K}_2\text{Sr}[\text{B}_4\text{O}_5(\text{OH})_4]_2 \cdot 10\text{H}_2\text{O}) \\ = 2\Delta_f G_m^o(\text{K}^+, \text{aq}) + \Delta_f G_m^o(\text{Sr}^{2+}, \text{aq}) \\ + 2\Delta_f G_m^o\{[\text{B}_4\text{O}_5(\text{OH})_4]^{2-}\} + 10\Delta_f G_m^o(\text{H}_2\text{O}, \text{l}) \end{aligned} \quad (3)$$

The thermodynamic parameters are listed in Table 2. We calculated Δ<sub>f</sub>H<sub>m</sub><sup>o</sup> of the K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·8H<sub>2</sub>O to be -10883.68 kJ mol<sup>-1</sup>. It can be seen that the calculated values are in good agreement with experimental results. The relative error is 0.19%.

Combining with the standard molar enthalpy of formation of K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(cr) in this work, and the standard molar Gibbs free energies Δ<sub>f</sub>G<sub>m</sub><sup>o</sup> of K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(cr) to be -9690.78 kJ mol<sup>-1</sup> from a group contribution method, the standard molar entropy of formation Δ<sub>f</sub>S<sub>m</sub><sup>o</sup> of K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(s) has also been calculated as -4070.74 J K<sup>-1</sup> mol<sup>-1</sup>, according to the

Table 1  
Thermochemical cycles and results for the derivation of Δ<sub>f</sub>H<sub>m</sub><sup>o</sup> (K<sub>2</sub>Sr[B<sub>4</sub>O<sub>5</sub>(OH)<sub>4</sub>]<sub>2</sub>·10H<sub>2</sub>O(cr), *T* = 298.15 K

Reaction	Δ <sub>f</sub> H <sub>m</sub> (kJ mol <sup>-1</sup> )
(1) K <sub>2</sub> Sr[B <sub>4</sub> O <sub>5</sub> (OH) <sub>4</sub> ] <sub>2</sub> ·10H <sub>2</sub> O(cr) + 161.39 (HCl·54.577H <sub>2</sub> O) = 2K <sup>+</sup> (aq) + Sr <sup>2+</sup> (aq) + 4Cl <sup>-</sup> (aq) + 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.989H <sub>2</sub> O)	129.82 ± 0.30
(2) 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.951H <sub>2</sub> O) = 8H <sub>3</sub> BO <sub>3</sub> (cr) + 157.39 (HCl·55.951H <sub>2</sub> O)	-174.64 ± 0.64 [15]
(3) 2K <sup>+</sup> (aq) + 2Cl <sup>-</sup> (aq) + 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.951H <sub>2</sub> O) = 2KCl(cr) + 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.951H <sub>2</sub> O)	-35.26 ± 0.22 [16]
(4) 2K <sup>+</sup> (aq) + Sr <sup>2+</sup> (aq) + 4Cl <sup>-</sup> (aq) + 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.989H <sub>2</sub> O) = SrCl <sub>2</sub> ·6H <sub>2</sub> O(cr) + 2K <sup>+</sup> (aq) + 2Cl <sup>-</sup> (aq) + 8H <sub>3</sub> BO <sub>3</sub> (aq) + 157.39 (HCl·55.951H <sub>2</sub> O)	-41.80 ± 0.11
(5) 157.39 (HCl·55.951H <sub>2</sub> O) = 157.39 (HCl·54.577H <sub>2</sub> O) + 216.254H <sub>2</sub> O(l)	4.03 ± 0.16 [17]
(6) 2H <sub>2</sub> (g) + 2Cl <sub>2</sub> (g) + 218.308H <sub>2</sub> O(l) = 4 (HCl·54.577H <sub>2</sub> O)	-661.72 ± 0.40 [17]
(7) SrCl <sub>2</sub> ·6H <sub>2</sub> O(cr) = Sr(cr) + Cl <sub>2</sub> (g) + 6H <sub>2</sub> (g) + 3O <sub>2</sub> (g)	2623.80 ± 0.16 [17]
(8) 2KCl(cr) = 2K(cr) + Cl <sub>2</sub> (g)	873.50 ± 0.20 [17]
(9) 2H <sub>2</sub> (g) + O <sub>2</sub> (g) = 2H <sub>2</sub> O(l)	-571.66 ± 0.08 [18]
(10) 8H <sub>3</sub> BO <sub>3</sub> (cr) = 8B(cr) + 12H <sub>2</sub> (g) + 12O <sub>2</sub> (g)	8758.40 ± 6.40 [18]
(11) K <sub>2</sub> Sr[B <sub>4</sub> O <sub>5</sub> (OH) <sub>4</sub> ] <sub>2</sub> ·10H <sub>2</sub> O(cr) = 2K(cr) + Sr(cr) + 8B(cr) + 14H <sub>2</sub> (g) + 14O <sub>2</sub> (g)	10904.47 ± 6.46

Table 2

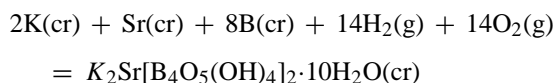
Thermodynamic parameters of borate polyanions and the experimental and calculated  $\Delta_f H_m^\circ$  and  $\Delta_f G_m^\circ$  of  $K_2Sr[B_4O_5(OH)_4]_2 \cdot 10H_2O(cr)$  at 295.15 K

Species	$\Delta_f H_m^\circ$ (kJ mol <sup>-1</sup> )	$\Delta_f G_m^\circ$ (kJ mol <sup>-1</sup> )
K <sup>+</sup> (aq) [19]	-252.38	-283.26
Sr <sup>2+</sup> (aq) [18]	-545.80	-559.48
H <sub>2</sub> O(l) [19]	-290.42	-237.28
[B <sub>4</sub> O <sub>5</sub> (OH) <sub>4</sub> ] <sup>2-</sup> [19]	-3464.46	-3095.99
K <sub>2</sub> Sr[B <sub>4</sub> O <sub>5</sub> (OH) <sub>4</sub> ] <sub>2</sub> ·10H <sub>2</sub> O(s)		
Calc.	-10883.68	-9690.78
Expt.	-10904.47	
Error (%)	0.19	

following equation:

$$\Delta_f S_m^\circ = \frac{\Delta_f H_m^\circ - \Delta_f G_m^\circ}{T} \quad (4)$$

And then, the standard molar entropy of  $K_2Sr[B_4O_5(OH)_4]_2 \cdot 10H_2O(cr)$  has been calculated to be 858.31 J K<sup>-1</sup> mol<sup>-1</sup>, on the basis of the following reaction:



The standard molar entropies of the elements were taken from NBS tables as 64.18, 52.30, 5.86, 130.684, and 205.138 J K<sup>-1</sup> mol<sup>-1</sup> for K(cr), Sr(cr), B(cr), H<sub>2</sub>(g), and O<sub>2</sub>(g), respectively.

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### Appendix A. Supplementary data

Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.tca.2007.08.004.

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